

Surname: _____ Name: _____ Student code: _____

**There is no need,
and actually, it is NOT allowed using the scientific calculator to make this test**

Section 1: QUIZ

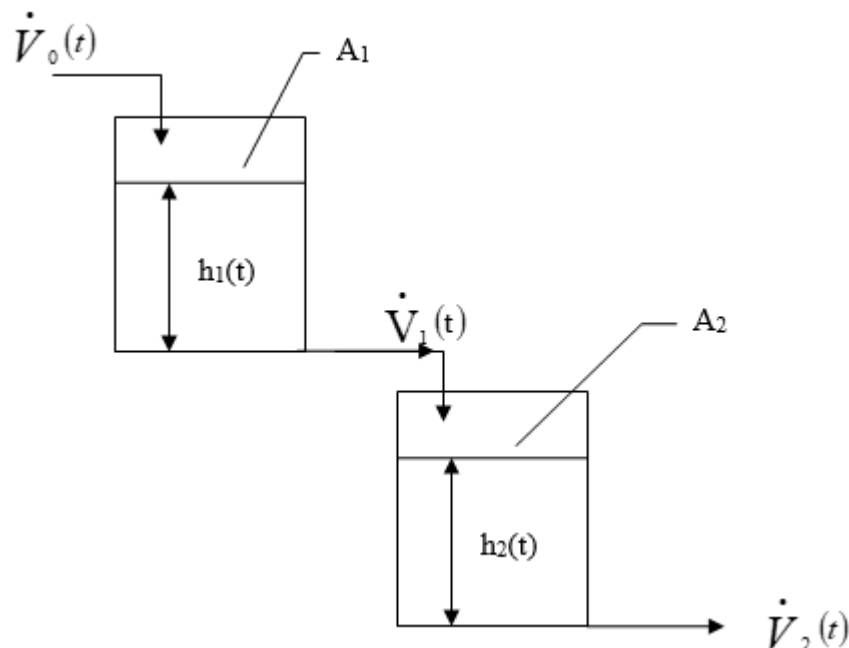
- 1) 1. The time constant τ_p of a 1st order system coincides with the time required for the step response to reach 50% from the final value
True False
- 2) The damping factor of a 2nd order system can also be negative
True False
- 3) The IAE calibration formula minimizes the integral of the error module
True False

Section 2: QUIZ

1. Which one of the following definitions does not apply to a **feedback controller**?
 - a. "direct action"
 - b. "reverse action"
 - c. a relay
 - d. FOPDT
2. The PI controller transfer function is
 - a. $G_c=K_c[1+ \tau_{IS}]$
 - b. $G_c=K_c[1+1/(\tau_{IS})]$
 - c. $G_c=K_c[1/(1+\tau_{IS})]$
 - d. $G_c=K_c/(\tau_{IS})$
3. Which of the following "parameters" is not included in the 2nd order system law?
 - a. Process gain
 - b. *overshoot*
 - c. Natural oscillation period
 - d. Damping factor
4. The offset is:
 - a. $y_\infty - y_{SP}(t)$
 - b. $y_{SP}(t) - y_\infty$
 - c. $y_\infty - y_m(t)$
 - d. Always positive

Section 3: DYNAMIC REFERENCE MODELS

3.1. Dynamic response of 2nd order



The system in the figure is formed by the two tanks in series operating each with a linear relationship between the output flow rate and the liquid level, with the following additional data:

$$A_1 = 2 \text{ m}^2 \quad A_2 = 1 \text{ m}^2 \quad R_1 = 1.5 \text{ m}/(\text{m}^3/\text{min}) \quad R_2 = 3 \text{ m}/(\text{m}^3/\text{min})$$

- What is the time constant of each tank?
- What is the static gain of each tank?

At steady state, the input flow rate is constant: $\dot{V}_{0s} = 1 \text{ m}^3/\text{min}$.

At time $t = 0$, the input flow rate into the first tank $\dot{V}_0(t)$ is sharply raised to $1.5 \text{ m}^3/\text{min}$ and then remains constant on such a new value. You want to know as a result of this change:

- how much the total variation will be in height of the 1st tank for a long time
- how long the level change of 1st tank takes to reach 95% of final variation
- how much the total variation will be in height of the 2nd tank for a long time
- how long the 2nd tank takes to reach 70% of its level variation

NB:

to answer these questions, you are asked to make use of the following generalized diagrams of the dynamic response and NOT to employ FORMULAS !

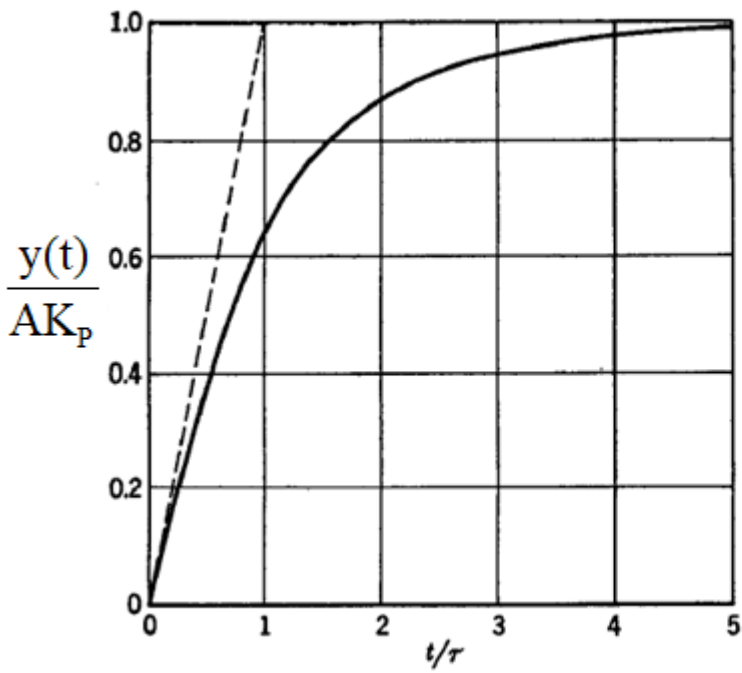
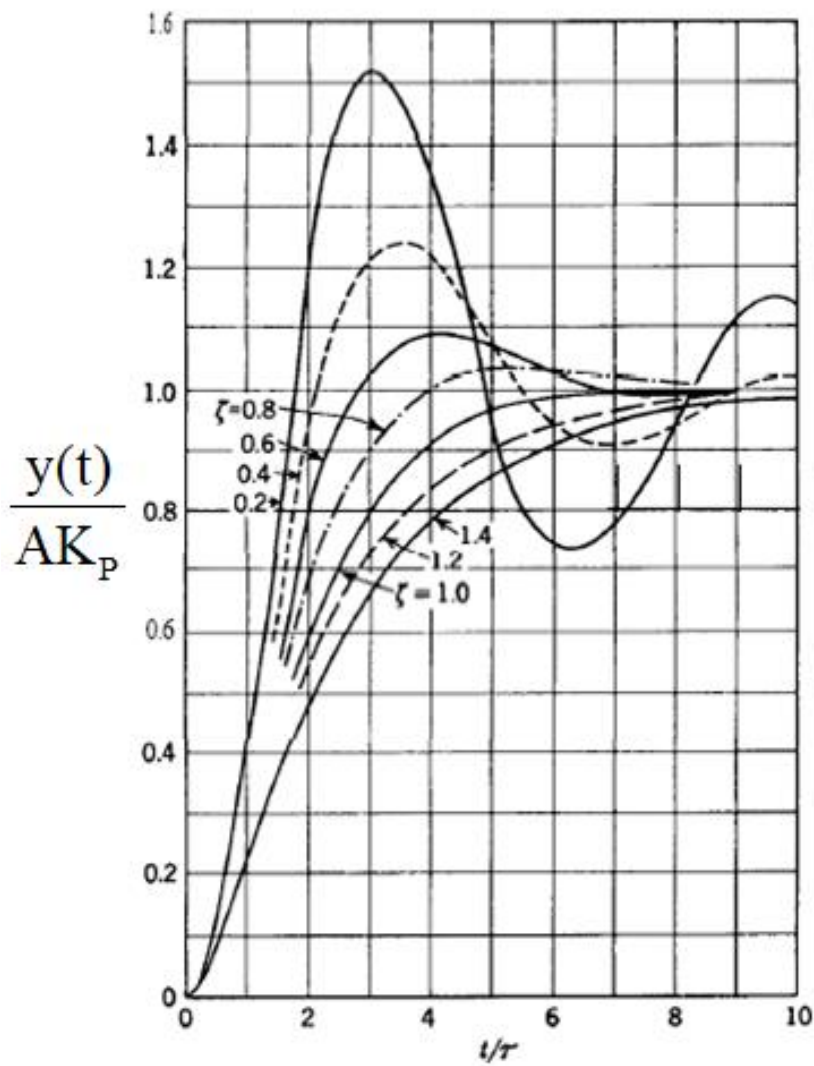


FIGURE 5-6
Response of a first-order system to a step input.



3.2. Poles and zeros of a transfer function

For the following **Transfer Function**

$$G(s) = \frac{s^2 + 1}{s^3 + 3s^2 + 2s}$$

- a) calculate the zeros of this TF
- b) calculate the poles of this TF
- c) draw the complex plane, and places each of the poles on it

For each of the poles

- d) provide the mathematical contribution it gives to the dynamic response in the time domain
- e) provide its stability properties in the time domain

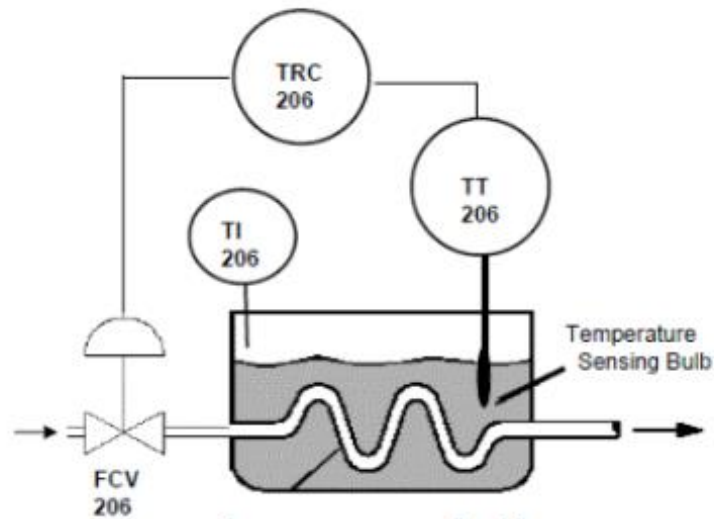
3.3. FOPDT Model

- a) How many and what are the characteristic parameters?
- b) What is the transfer function
- c) Is it a linear model?
- d) Some people define it as a **series system**: Why? Which dynamic reference models do make it?
- e) In the case of a FOPDT INTEGRATING model, how many and what are the characteristic parameters?
- f) Also in the case of a FOPDT INTEGRATING model, what is the transfer function?

Section 4: PROCESS CONTROL

4.1. Feedback control

The figure introduces a practical application of feedback control by means of a simplified P&ID.



Among the various variables (flow rate, etc.)

- select the **controlled variable**:
- select the **manipulated variable**:
- select the **disturbance variable** (if any):
- Define the role that each control **block component** has in the Feedback Block Diagram, and that is specific to the case in question
 - liquid tank:
 - pipe:
 - valve FCV 206:
 - TI 206:
 - TT 206:
 - TRC 206:
- ~~What kind of **signals** is used for communication in this case of **feedback control**?~~

Section 5: CONTROLLERS**5.1. The relay controller**

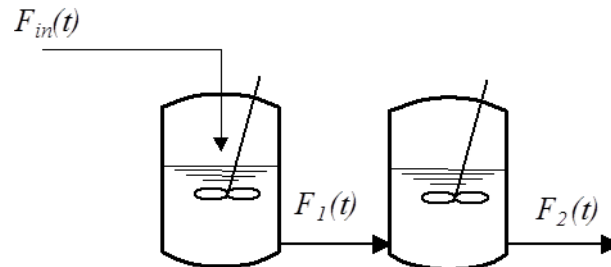
- a) draw the **error** $\varepsilon(t)$ – *controller output* $o(t)$ diagram in presence of **hysteresis**

- b) explain briefly what **hysteresis** is

- c) provide an application example of a *relay controller*

Section 6: MATHEMATICAL MODELS**6.1. Development of a dynamic mathematical model for a lumped parameter system**

With ref. to the dynamic system corresponding to the case in figure:



under the **hypotheses** of

- linear outflow relationship
- isothermal operation

- determine the overall **transfer function** $G_{ov}(s) = h_2(s)/F_{in}(s)$
- determine the **transfer function** of the 1st tank $G_1(s) = h_1(s)/F_{in}(s)$