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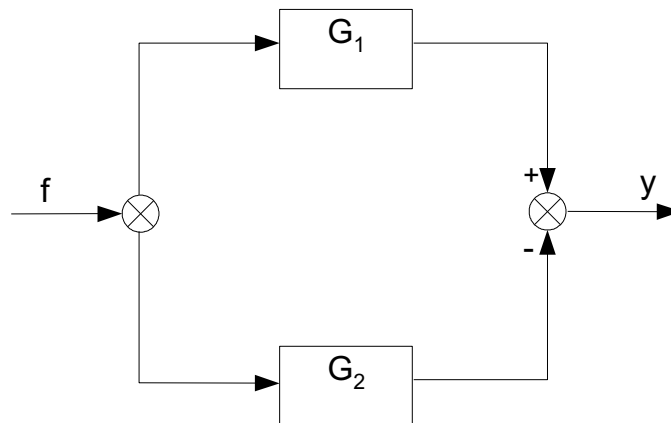
Name

student ID No.:

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## Section 4: STABILITY OF LINEAR DYNAMIC SYSTEMS

A linear dynamic system is made of two processes in this way



with transfer functions  $G_1(s) = \frac{\left(\frac{1}{16}\right)}{s+0.95}$        $G_2(s) = \frac{1}{\frac{s}{1.95}+1.05}$

where:

$p$  is a parameter

- I. Determine the system  $G_p(s)$  resulting from the parallel.
- II. Which order is  $G_p(s)$ ?
- III. Assign a value to the parameter  $p$  such as the system  $G_p(s)$  resulting from the parallel becomes an **inverse-response system**
- IV. How much is the **gain** for such a system  $G_p(s)$  resulting from the parallel?

### Part A: Root locus

For the **system**  $G_p(s)$ , use Matlab and SisoTool resources, attach here their results and answer the following questions:

1. Plot the *root locus*
2. Discuss existence of asymptotes and, if possible, calculate the gravity center and angles formed with the real axis.
3. Calculate the limiting value/values for  $K_c$

For the **system**  $G_p(s)$ , add a PD controller:

4. Plot the new *root locus*
5. Calculate the new limiting value/values for  $K_{cD}$

6. Compare  $K_{cD}$  to  $K_c$  and discuss if the “stability space” is increased or not

For the **system**  $G_p(s)$ , add a PI controller:

7. Plot the new *root locus*
8. Calculate the new limiting value/values for  $K_{cl}$
9. Compare  $K_{cl}$  to  $K_c$  and discuss if the “stability space” is increased or not

## Part B: Frequency response

For the **dynamic system**  $G_p(s)$  and a ***P controller*** with  $K_c=1$ :

- 1) Plot the **asymptotic Bode Diagrams** by means of the ASBODE script, and attach them here
- 2) Does a *crossover* frequency exist? How much is it?
- 3) Does a *gain crossover* frequency exist? How much is it?
- 4) Decide if the Bode stability criterion is applicable
- 5) If yes, is the above system closed-loop stable?

## Part C: Dynamic responses in the time domain

Come back to the original system  $G_p(s)$  resulting from the parallel:

- A. assign a new value to the parameter  $p$  such as  $G_p(s)$  is NOT an **inverse-response system** anymore
- B. plot the **open-loop** dynamic response to a unit step, attach it here and give your comments
- C. assign a **P controller** with  $K_c=0.1$  and plot the **closed-loop** dynamic response to a unit step change in *set point*, attach it here and give your comments

## Part D: Inverse Response Compensator

- a) write its TF