

Last name

Name

student ID No.:

Section 4: STABILITY OF LINEAR DYNAMIC SYSTEMS

A dynamic process $G_p(s)$ is the result of 2 linear systems in series, each having the following transfer function

$$G_1(s) = \frac{n + 0.15}{n - 0.15} \frac{1}{s^3}$$

$$G_2(s) = \frac{1}{10} \frac{\left(\frac{s}{0.2} + 1\right)^2}{\left(\frac{s}{4.5} \cdot \frac{n + 0.15}{n - 0.15} + 1\right)^2}$$

where $n = \text{PC No.}$

- I. Determine all open loop **poles** and **zeroes**
- II. Determine all **time constants** in the polynomials at numerator and denominator
- III. How much is the **type g**?
- IV. Is there any **damping factor**? If there is, how much is ζ ?

Part A: Root locus

By using as much as possible the Matlab and SisoTool resources, answer here the following questions:

- A1. Explain if you've to use **direct or inverse** Root Locus rules
- A2. Plot the *root locus* by means of Matlab and SisoTool resources and attach it here
- A3. Calculate, if possible, the value/values of the critical gain K^*

Part B: Frequency response

For the **original dynamic system** $G_p(s)$ reported on top, with $K_c = 1$:

- B1. Plot the **Bode Diagrams** by means of Matlab resources and attach them here

- B2. Does a *crossover* frequency exist? How much is it?
- B3. Does a *gain crossover* frequency exist? How much is it?
- B4. Decide if the Bode stability criterion is applicable
- B5. If yes, is the above system closed-loop stable?
- B6. Plot and attach here the **extended Nyquist diagram** *together with the unit circle and the Peak Response* by means of Matlab and SisoTool resources, then discuss it in details
- B7. Check, on the base of the **Nyquist** stability criterion, if the above system is closed-loop stable
- B8. By means of the **gain margin**, calculate the limiting value $K_{c,lim}$ and compare it with the previously found value K^*

Part C: Dynamic responses in the time domain

For the **dynamic system** $G_p(s)$ with $K_c=5$:

- C1. Plot the **closed loop response** to a unit step change in the **set point**, attach it here and give your comments

For the **dynamic system** $G_p(s)$ with $K_c=0.05$:

- C2. Plot the **closed loop** time profile of the **manipulated variable** to a unit step change in the **set point**, attach it here and give your comments

Part D: = = =

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