

Last name

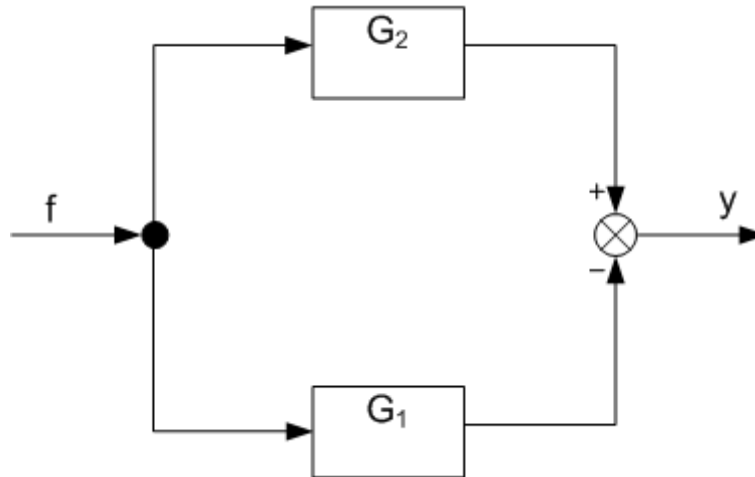
Name

student ID No.:

PC No. \_\_\_\_\_

## Section 4: STABILITY OF LINEAR DYNAMIC SYSTEMS

A linear dynamic system is made of two processes in this way



with transfer functions:

$$G_1(s) = (-1)^n \frac{2}{\frac{n}{4}s + 1.05}$$

$$G_2(s) = (-1)^n \frac{3}{\frac{n}{2}s + 0.995}$$

where:

$$n = \text{PC No.}$$

- I. Reduce each TF above to the non-Factorized Form with the trailing coefficient equal to unity
- II. Is the system  $G_p(s)$  resulting from the parallel is an **inverse-response system**? Why?
- III. How much is the **gain** for such as a system  $G_p(s)$  resulting from the parallel?
- IV. Plot the system  $G_p(s)$  response to a unit step change in  $f(s)$  and verify if it is actually "inverse"

### Part A: Root locus

By using as much as possible the Matlab or SisoTool resources, answer here the following questions:

1. Explain if you've to use **direct or inverse** Root Locus rules
2. Plot the *root locus* by means of Matlab or SisoTool resources and attach it here

3. Determine, if any, and comment the **loci** on the real axis
4. Calculate, if any, and comment the value/values of the **critical gain**  $K^*$

### Part B: Frequency response

For the **dynamic system**  $G_p(s)$  and a  **$\mathcal{P}$  controller** with  $K_c=1$ , by using as much as possible the Matlab or SisoTool resources, answer here the following questions:

- 1) Plot the **asymptotic Bode Diagrams** by means of the ASBODE script, and attach them here
- 2) Decide if the Bode stability criterion is applicable
- 3) If yes, is the above system closed-loop stable?

### Part B bis: Frequency response

For the **dynamic system**  $G_{pbis}(s)$

$$G_{pbis}(s) = G_p(s) e^{-\frac{n}{4}s}$$

where:

$$n = \text{PC No.}$$

and a  **$\mathcal{P}$  controller** with  $K_c=1$ , by using as much as possible the Matlab or SisoTool resources, answer here the following questions, when the two transfer functions are changed as follows:

- 1) Plot the **extended Nyquist diagram** *together with the unit circle and the Peak Response* by means of Matlab resources, attach it here and give your comments in details
- 2) Check, on the base of the **Nyquist** stability criterion, if the above system is closed-loop stable
- 3) determine the **gain** margin, if any
- 4) determine the **phase** margin, if any

### Part C: Dynamic responses in the time domain

For the **dynamic system**  $G_{pbis}(s)$  and a  **$\mathcal{P}$  controller** with  $K_c=0.15$ :

- 1 - Plot the **open loop response** to a unit step **input** change, attach it here and give your comments

**Part D: compensation**

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