
Last name**Name****student ID No.:**

PC No. _____

Section 4: STABILITY OF LINEAR DYNAMIC SYSTEMS

A linear dynamic process has the following transfer functions:

$$G_2(s) = \frac{(s + 1)}{\left(s - 2 \cdot \left(\frac{n - 0.05}{n + 0.05}\right)\right)} e^{-4 \cdot \left(\frac{n - 0.05}{n + 0.05}\right)s}$$

where:

n = N. matricola (student ID No.)

- I. Is $G_2(s)$ a BIBO stable system at **open-loop**?
- II. How much is the **gain**?
- III. Is $G_2(s)$ an **inverse-response system**?

Part A: Root locus

For the open loop TF $G_2(s)$, answer the following questions aimed at focusing the Padé approximation:

- A1. Use a 1st order Padé approximation, plot the *root locus* by means of Matlab or SisoTool resources and attach it here
- A2. Calculate the limiting value/values K_1^* , if any
- A3. Use a 2nd order Padé approximation, plot the *root locus* by means of Matlab or SisoTool resources and attach it here
- A4. Calculate the limiting value/values K_2^* , if any
- A5. Use a 3rd order Padé approximation, plot the *root locus* by means of Matlab or SisoTool resources and attach it here

A6. Calculate the limiting value/values K_3^* , if any

A7. By comparing all of the above results for the *root locus*, provide a short and reasoned comment

Part B: Frequency response

For the open loop TF $G_2(s)$ and $\mathcal{K}c=I$, answer the following questions:

B1) Use a 1st order Padé approximation, plot the **Bode Diagrams** by means of Matlab or SisoTool resources, with a *log scale of the magnitude (NOT in dB)*, and attach them here

B2) Use a 2nd order Padé approximation, plot the **Bode Diagrams** by means of Matlab or SisoTool resources, with a *log scale of the magnitude (NOT in dB)*, and attach them here

B3) Use a 3rd order Padé approximation, plot the **Bode Diagrams** by means of Matlab or SisoTool resources, with a *log scale of the magnitude (NOT in dB)*, and attach them here

B4) Come back to the original TF $G_2(s)$, plot the **Bode Diagrams** by means of Matlab resources, with a *log scale of the magnitude (NOT in dB)*, and attach them here

B5) Calculate the value of each TF in both **polar coordinates** (AR, ϕ) and **cartesian coordinates complex number** ($a + jb$) just corresponding to a given $\omega = 100$ rad/s, for all of the above four cases above

B6) By comparing all of the above results for the **Bode Diagrams**, provide a short and reasoned comment

B7) Use a 1st order Padé approximation, plot the **extended Nyquist Diagram** by means of Matlab or SisoTool resources, *together with the unit circle and the Peak Response*, and attach it here

B8) Is the above **Nyquist diagram** crossing the **critical point**?

B9) Check, on the base of the **Nyquist stability criterion**, if the above system is closed-loop stable

- B10) Come back to the original TF $G_2(s)$, plot the **extended Nyquist Diagram** by means of Matlab or SisoTool resources, *together with the unit circle and the Peak Response*, and attach it here
- B11) By comparing the above two **Nyquist Diagrams**, provide a short and reasoned comment

Part C: Dynamic responses in the time domain

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Part D:

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