

Last name

Name

student ID No.:

PC No. \_\_\_\_\_

## Section 4: STABILITY OF LINEAR DYNAMIC SYSTEMS

A linear dynamic process  $G_p(s)$  has the following 4 **poles**:

$$\begin{aligned} &0 \\ &-0.05*(2*n+0.5)/(2*n-0.5) \\ &-0.1 \\ &-2 \end{aligned}$$

the following 2 **zeroes**:

$$\begin{aligned} &-1 \\ &-0.5*(2*n+0.5)/(2*n-0.5) \end{aligned}$$

the following **transfer constant**:

$$k = -1$$

where:

$$n = N. \text{ matricola (student ID No.)}$$

- I. Is  $G_p(s)$  a BIBO stable system at **open-loop**?
- II. Is  $G_p(s)$  an **inverse-response system**?
- III. How much is the **type “g”**?

### Part A: Root locus

For the open loop TF  $G_p(s)$ ,

A1. Plot the root locus by means of Matlab and SisoTool resources and attach it here

A2. Discuss calculate and, if any, the **breakaway points**

A3. Discuss calculate and, if any, the limiting value/values  $K^*$

A4. After reconsidering the original 4 **poles**, suggest which one you would eliminate in order to improve the closed loop stability to the best possible

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## Part B: Frequency response

For the open loop TF  $G_p(s)$  and  $\mathcal{K}C=I$ , answer the following questions:

- B1) Plot the **Bode Diagrams** by means of Matlab/SisoTool resources, with a *log scale of the magnitude (NOT in dB)*, and attach them here
- B2) With ref to the **Bode Diagrams** of the **phase**, discuss its pattern and provide a short and reasoned comment
- B3) Decide if the **Bode stability criterion** is applicable
- B4) If yes, is the above system closed-loop stable?
- B5) Plot and attach here the **extended Nyquist diagram together with the unit circle and the Peak Response** by means of Matlab and SisoTool resources, then discuss it in details
- B6) Is the above **Nyquist diagram** crossing the **critical point**?
- B7) Check, on the base of the **Nyquist stability criterion**, if the above system is closed-loop stable
- B8) Calculate the value of TF  $G_p(s)$  in **polar coordinates** ( $AR, \phi$ ) at a given  $\omega = 0.5$  rad/s
- B9) Calculate the value of TF  $G_p(s)$  in **cartesian coordinates** as a **complex number** ( $a + jb$ ) at a given  $\omega = 0.6$  rad/s

## Part C: Dynamic responses in the time domain

- C1. plot the **open-loop** dynamic response to impulse, attach it here and give your comments
- C2. plot the **closed-loop** dynamic response to an impulse in **set point**, attach it here and give your comments

C3. plot the **closed-loop** dynamic response to an impulse in **process disturbance** (input named **du**), attach it here and give your comments

**Part D:**

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