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**Last name****Name****student ID No.:**

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**PC No.** \_\_\_\_\_

## Section 4: STABILITY OF LINEAR DYNAMIC SYSTEMS

A linear dynamic process has the following transfer function:

$$G_p(s) = 1.3889 \frac{(n - 0.05)}{(n + 0.05)} \cdot \frac{(s + 1)(s + 0.8333)}{s(s + 0.08333)/(s + 0.1)}$$

where:

**n = N. matricola (student ID No.)**

- I. Which **order** is the system  $G_p(s)$ ?
- II. Is  $G_p(s)$  a BIBO stable system at **open loop**?
- III. Convert  $G_p(s)$  into the **canonical form**

### Part A: Root locus

For the open loop TF  $G_{OL}(s)$ , use Matlab and SisoTool resources, attach here their results and answer the following questions:

A1. Plot the *root locus* by means of Matlab or SisoTool resources and attach it here

A2. Calculate, if any, the **breakaway points** and discuss them

A3. Calculate, if any, the limiting value/values  $K^*$  and discuss them

A4. Calculate, if any, the value of **all closed loop poles** just corresponding at  $K^*$

A5. Provide an example of a completely different rational transfer function  $SYS(s)$  that has the root locus with the property that no trajectory lies on the real axis

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## Part B: Frequency response

For the same **dynamic system**  $G_p(s)$   
and  $\mathcal{K}C=I$ ,

use Matlab and SisoTool resources, attach here their results and answer the following questions:

B1) Plot the **Bode Diagrams** by means of Matlab resources, with a *log scale of the magnitude (NOT in dB)*, and attach them here

B2) Does a *resonance* frequency exist? How much is it?

B3) Decide if the **Bode stability criterion** is applicable

B4) If yes, is the above system closed-loop stable?

B5) Plot the extended Nyquist diagram together with *the unit circle and the Peak Response*, and attach it here

B6) Is the Nyquist diagram crossing the **critical point**?

B7) Check, on the base of the Nyquist stability criterion, if the above system is closed-loop stable

B8) Calculate the value of  $G_p(j\omega)$  as a **complex number** just corresponding to a phase angle  $\phi=\pi$  rad

## Part C: Dynamic responses in the time domain

For the same **dynamic system**  $G_p(s)$   
and  $\mathcal{K}C=I$ ,

use Matlab and SisoTool resources, attach here their results and answer the following questions:

C1) Plot the **open loop response** to an **impulse** input change, attach it here and give your comments

C2) Plot the **closed loop response** to an **impulse** input change in **disturbance**, attach it here and give your comments

**Part D:**

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