

Last name

Name

student ID No.:

## Section 4: STABILITY OF LINEAR DYNAMIC SYSTEMS

A dynamic process  $G_p(s)$  has the following 5 **poles**:

$$\begin{aligned} & j \\ & -j \\ & -0.05*(n-0.05)/(n+0.05) \\ & -0.1 \\ & -2 \end{aligned}$$

the following 2 **zeroes**:

$$\begin{aligned} & -(n-0.05)/(n+0.05)*(0.5+j) \\ & -(n-0.05)/(n+0.05)*(0.5-j) \end{aligned}$$

the following **transfer constant**:

$$1$$

where:

$$n = \text{PC No.}$$

- I. How much is the **gain** for  $G_p(s)$ ?
- II. How much is the **type g** for  $G_p(s)$ ?
- III. Is this an **inverse response** system?

### Part A: Root locus

For the **dynamic system**  $G_p(s)$ , by using as much as possible the Matlab or SisoTool resources, answer here the following questions:

- a) Explain if you've to use **direct or inverse** Root Locus rules
- b) Plot the *root locus* by means of Matlab or SisoTool resources and attach it here
- c) Calculate, if any, the **breakaway points**
- d) Calculate, if any, and comment the value/values of the **critical gain  $K^*$**
- e) Calculate the values of the closed loop poles for **gain  $K_c=2$**
- f) Select one or two **poles** in  $G_p(s)$  that you consider responsible of **closed loop instability** and *propose a numerical change for them*, which you consider, based on your judgement, more favorable to **closed loop stability**

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## Part B: Frequency response

By using as much as possible the Matlab or SisoTool resources, answer here the following questions:

- 1) Plot the *Asymptotic Bode Diagrams*, attach them here and give your comments in details
- 2) Does a **resonance** frequency exist? How much is it?
- 3) Calculate *precisely* AR and  $\phi$  at  $\omega=2$  rad/s
- 4) Decide if the **Bode stability criterion** is applicable
- 5) If yes, is the above system closed-loop stable?
- 6) Plot the **extended Nyquist diagram** of  $G_p(s)$  *together with the unit circle and the Peak Response* by means of Matlab resources, attach it here and give your comments in details
- 7) Check, on the base of the **Nyquist** stability criterion, if the above system is closed-loop stable

## Part C: Dynamic responses in the time domain

For the **original dynamic system**  $G_p(s)$ :

- 1) plot the **open loop** system dynamic response to an **impulse** change in *input* by means of Matlab resources, attach it here and give your comments.
- 2) plot the **closed loop** system dynamic response to an **impulse** change in *disturbance* by means of Matlab resources, attach it here and give your comments.

## Part D:

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